

Implementation of non-linear gauge in GRACE

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Introduction

- Systems for Automatic Computation of cross sections → essential tools in HEP
 - Complicated calculation
 - EW, susy : many particles and vertices
 - final states: multi-body
 - high statistics: higher-order(loops)
- **Beyond man-power**

Automatic systems

- Diagram generation for the input process
- Amplitude/Matrix element generation
- Kinematics and Integration (efficiency)
- Event generation (efficiency & weight)
- Peripheral tools: rule generator, diagram selection, QED radiation, PDF, loop integral library, multi-process, color flow and interface for hadronization, etc.

Automatic Computation

- ⇒ Automatic calculation of cross sections in HEP.
- ⇒ Large scale computation beyond man-power.
- ⇒ Essential tools for current and future HEP.

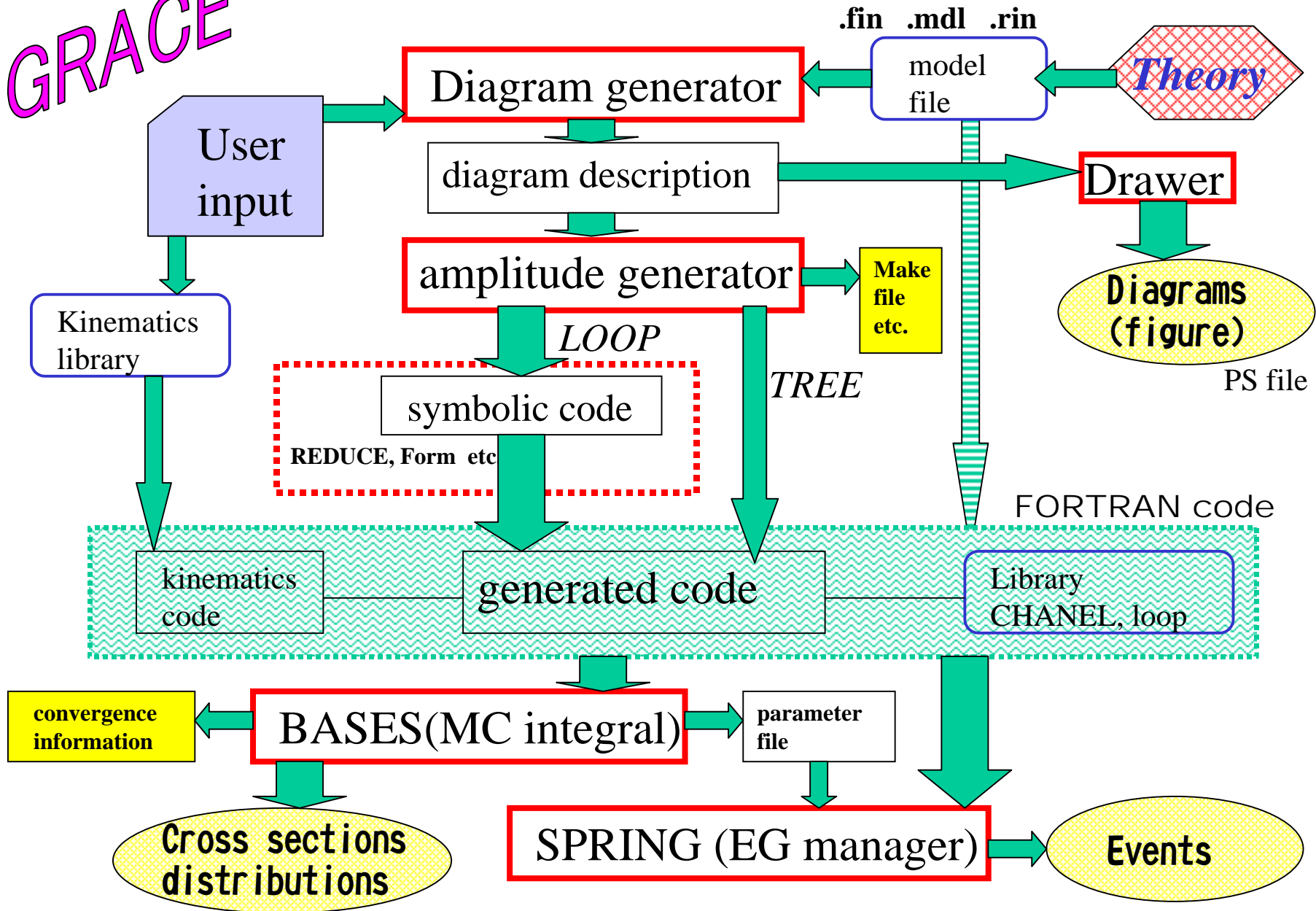
1. Automatic computation systems working in the world

ALPHA(Italy), CompHEP(Russia), FDC(China), FeynArts/FeynCalc series(Germany), GEFICOM(Germany/Russia), GRACE(Japan), MadGraph(USA), NIKHEF setup(Holland) ...

2. Examples of Achievements

- 4-fermion generators(76 processes) for LEP-2 experiments(ALPHA,CompHEP, GRACE).
- $e^-e^+ \rightarrow 6\text{-fermion}$ (ALPHA,GRACE), $e^-e^+ \rightarrow \tilde{\chi}_1^0 \tilde{\chi}_1^0 q_1 \bar{q}_2 q_3 \bar{q}_4$ (GRACE), $\gamma\gamma \rightarrow 4\text{-fermion}$ (CompHEP).
- $ep \rightarrow el^+l^-X$ (GRACE).
- $p\bar{p} \rightarrow Wb\bar{b}j$ (CompHEP), $pp \rightarrow W^+W^-b\bar{b}j$ (MadGraph), $gg, q\bar{q} \rightarrow 8g$ (ALPHA).
- 1-loop calculation for $e^-e^+ \rightarrow W^-W^+$, $\gamma\gamma \rightarrow W^+W^-$, $W^+W^- \rightarrow W^+W^-$ (FeynArts/FeynCalc,GRACE), $e^-e^+ \rightarrow W^+\mu^-\bar{\nu}_\mu$ (GRACE).
- Hadronic Higgs decay in $O(\alpha_s^2)$, $O(\alpha\alpha_s)$ corrections to $Z \rightarrow b\bar{b}$, etc. (GEFICOM).
- 4-loop β -function($\sim 50,000$ diagrams) (NIKHEF setup).

GRACE



Introduction

- **How to check** (or how to believe) the results of automated systems ?
- Consistency checks:
Change particle assignment (kinematical),
Renormalization, IR cancellation,
Gauge invariance, ...

Very Powerful

NOTE: *Best check*
comparison between
systems == International
collaboration

Check by gauge invariance

- **Tree case** : Unitary gauge vs. covariant gauge.

- **Loop case**: Unitary gauge $-g^{\mu\nu} + (1-\xi)\frac{p^\mu p^\nu}{p^2 - \xi M^2}$ is not good for loop integrals
(Loop system includes loop integral libraries. The 'tHooft-Feynman gauge would be the unique choice.)

$$\gamma\gamma \rightarrow WWZ$$

Tree

Covariant gauge
vs. unitary gauge
calculation

$$\text{ans1/ans2-1} \\ = -9.992 * 10^{-16}$$

double precision

The report from gauge check for the process $\gamma\gamma \rightarrow W^+W^-Z$ (tree).

```
ans1 = 697.3329568147916
ans2 = 697.3329568147923
ans1/ans2 - 1 = -9.992007221626409E-16
```

Squared values of each amplitude are shown below. Here gauge parameters are $\xi_W = 2, \xi_Z = 3, \xi_A = 4, \xi_S = 5$ for the covariant gauge and all $\xi \rightarrow \infty$ in the unitary gauge.

Graph	Covariant G.	Unitary G.
1	21528.57045977585	18564.51167868807
2	.1460009958034371	--
3	2.692211734656595E-02	--
4	.1599975851326383	--
5	19057.88659999488	17008.20822853434
6	4.500684937408190E-03	--
7	3.373657195693665E-03	--
8	2.387622808895325E-02	--
9	323738.2044061869	470708.2532091573
10	.1600687342398619	--
11	9.569409743430992E-02	--
12	6.56115147597876	--
13	76805.68964151866	96110.62012296795
14	1.43800275181183	--
15	.701986206743452	--
16	.2135934480883664	--
17	26658.66122539515	37143.11975960149
18	.1397980786507487	--
19	3.933033557902666E-02	--
20	.2337393687908884	--
21	13193.5606871605	20773.43462811679
22	.180736158674087	--
23	4.112975720574200E-04	--
24	2.820012669875999E-02	--
25	5413.970868959231	4726.36532333212
26	103878.9857062928	155477.022786 222
27	2561.394063080011	4068.109238953077
28	5003.08499786053	9580.555716575343
29	4947.7452831425	4903.632157535491
30	12619.4389111047	16208.36717994843

Non-linear gauge

- Include several gauge parameters

$$\tilde{\alpha}, \tilde{\beta}, \tilde{\delta}, \tilde{\varepsilon}, \tilde{\kappa}$$

- Numerator structure is the same as

Feynman gauge $g^{\mu\nu}$ (for $\xi = 1$)

- Vertices modified (e.g. $\tilde{\alpha} = 1 \Rightarrow$ no $AW\chi$)
- New vertices (ghost sector) appear

Non-linear gauge fixing terms

$$\mathcal{L}_{\text{GF}} = -\frac{1}{\xi_W} F^+ F^- - \frac{1}{2\xi_Z} (F^Z)^2 - \frac{1}{2\xi} (F^A)^2$$

$$F^\pm = \left(\partial^\mu \mp i e \tilde{\alpha} A^\mu \mp i \frac{e c_W}{s_W} \tilde{\beta} Z^\mu \right) W_\mu^\pm \quad F^A = \partial^\mu A_\mu$$

$$+ \xi_W \left(M_W \chi^\pm + \frac{e}{2s_W} \tilde{\delta} H \chi^\pm \pm i \frac{e}{2s_W} \tilde{\kappa} \chi_3 \chi^\pm \right)$$

$$F^Z = \partial^\mu Z_\mu + \xi_Z \left(M_W \chi_3 + \frac{e}{2s_W c_W} \tilde{\epsilon} H \chi_3 \right)$$

Samples of NLG Feynman rules

W – W – A

$$e[g^{\mu\nu} (p_1 - p_2)^\rho$$

$$+ (1 + \tilde{\alpha} / \xi_W)(p_3^\nu g^{\mu\rho} - p_3^\mu g^{\nu\rho})$$

$$+ (1 + \tilde{\alpha} / \xi_W)(p_2^\mu g^{\nu\rho} - p_1^\nu g^{\mu\rho})]$$

W – χ – A

$$\mp ieM_W(1 - \tilde{\alpha})g^{\mu\nu}$$

modified

$\bar{c}^\mp - c^A - A - W^\pm$

$$- e^2 \tilde{\alpha} g^{\mu\nu}$$

$\bar{c}^\mp - c^A - \chi^\pm - H$

$$\mp ie^2 \frac{1}{2s_W} \tilde{\delta} \xi_W$$

New: ghost-ghost- VV/SS

Examples of results(1-loop)

$W=500\text{GeV}, \cos \theta = 0.985, k_{\text{cut}}=10\text{GeV}$

$M_z=91.187\text{GeV}, M_w=80.37, M_t=174, M_H=100, \lambda =1.d-15$

NLG : $\tilde{\alpha} = 2, \tilde{\beta} = 3, \tilde{\delta} = 4, \tilde{\epsilon} = 5, \tilde{\kappa} = 6$

$e^+e^- \rightarrow t\bar{t}$

TREE 0.5194160300

LG, $C_{\text{uv}}=0$: -0.168187331181333555

NLG, $C_{\text{uv}}=10$: -0.168187331181313571

#graphs

tree : 4

1-loop:150

$\frac{d\sigma}{d\cos\theta}$ (pb)

Examples of results(1-loop)

$W=500\text{GeV}, \cos \theta = 0.985, k_{\text{cut}}=10\text{GeV}$

$M_z=91.187\text{GeV}, M_w=80.37, M_t=174, M_H=100, \lambda =1.d-15$

NLG : $\tilde{\alpha} = 2, \tilde{\beta} = 3, \tilde{\delta} = 4, \tilde{\epsilon} = 5, \tilde{\kappa} = 6$

$W^+ \gamma \rightarrow t \bar{b}$

TREE 22.36869289

LG, CUV=0 : 0.832925006031624005

NLG, CUV=10: 0.832925006101842946

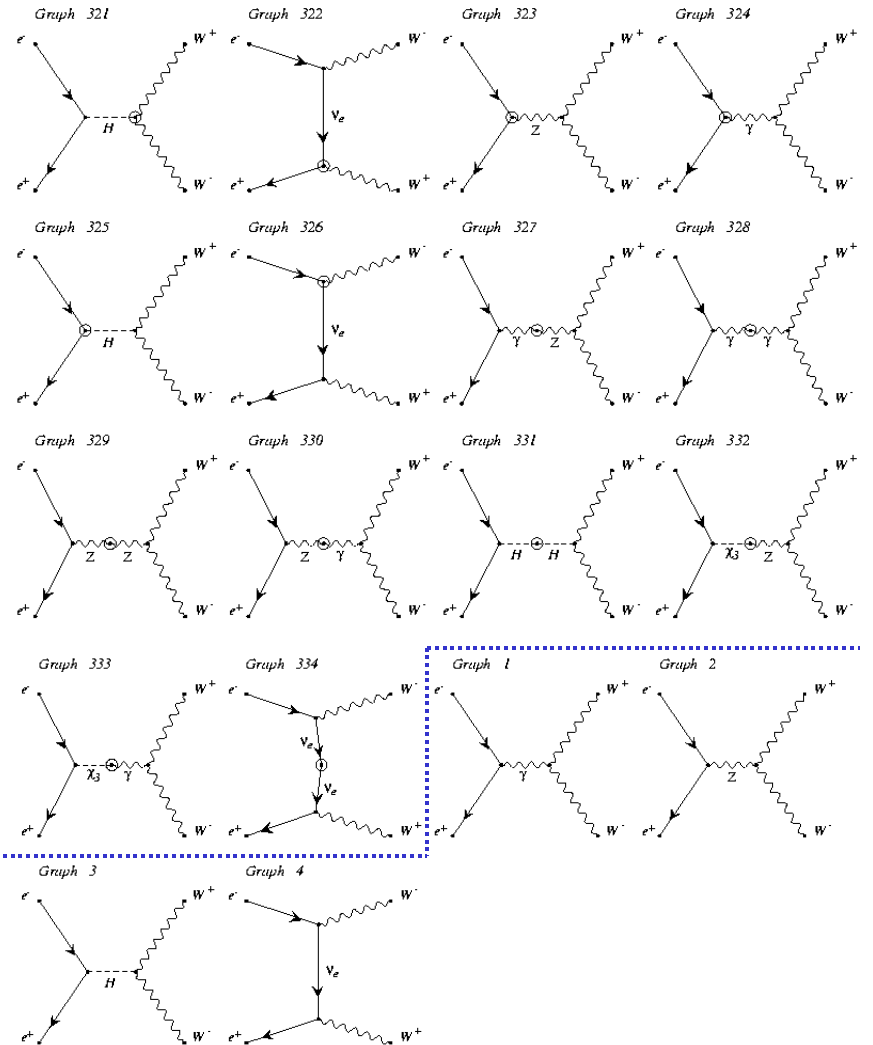
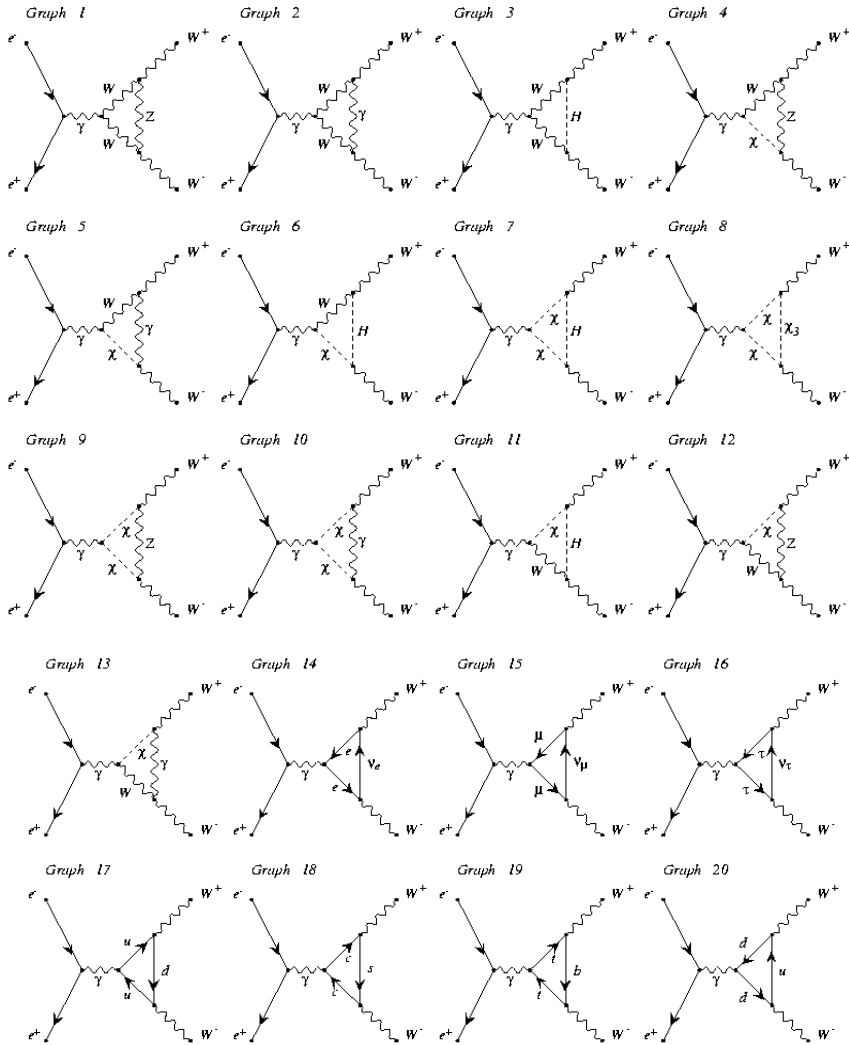
#graphs

tree : 4

1-loop:239

$\frac{d\sigma}{d\cos\theta}$ (pb)

diagrams drawn by GRACEFIG



$$e^-e^+ \rightarrow W^-W^+$$

$$e^-e^+ \rightarrow W^-W^+$$

#graphs

tree : 4

1-loop:334

TREE (TOTAL) : 75.071649720

LG, $C_{UV} = 0$: -15.4257567057010476

NLG, $C_{UV} = 10$: -15.4257562685176595

	LG	NLG
1) final vtx A	: -0.110232876612731998	-0.962735342032220331
2) final vtx Z	: -0.176836959641807318	-1.45399925309897249
3) final vtx H	: -0.731865348125769495E-011	-0.486300610973687554E-011
4) final vtx X3	: -0.147685555367555172E-013	-0.147685555367554793E-013
5) t-channel e+	: -102.919001290744660	-136.855066683011671
6) init vtx Z	: -6.93496613930373318	-6.82256179700717080
7) init vtx A	: -4.28572899550046760	-4.26803489737576847
8) init vtx H	: -0.136320409418589835E-009	-0.135363696968451092E-009
9) box	: -32.3611802623685705	37.7599169853874841
10) t-channel e-	: -102.919001309649019	-136.855066697757337
11) Renorm. SE:	0.191341031608370238	-0.580586801361939048E-001

Conclusion

- NLG is implemented into GRACE 1-loop system.
- Performance is good for the check of complicated calculation.
- To be used for the large scale calculation to confirm the output.