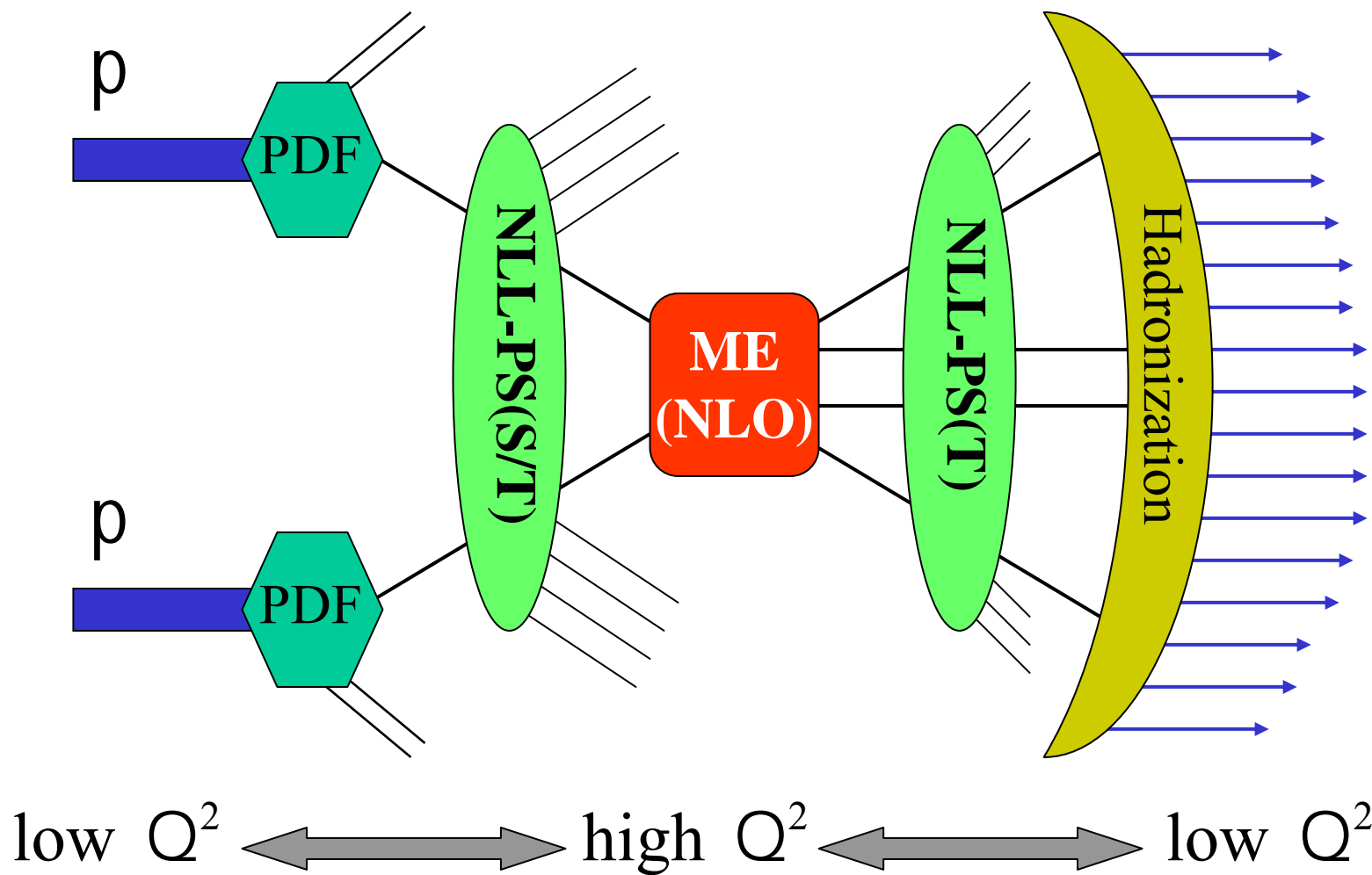


QCD and NLL-PS

CPP 2001, Tokyo, 2001.11.28-30

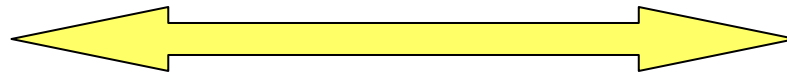
K.Kato (Kogakuin Univ.)

followed by Kurihara's talk



QCD

low Q^2



high Q^2

empirical model
soft physics

pert.QCD
reliable theoretical
prediction

RGE



try to use maximum
information of pert.QCD



The Art of Pert.QCD

- Many detailed theoretical predictions in literatures: LO, NLO, NNLO,...
for cross sections, shape parameters, distribution functions, ...
- The required stage is to construct event generators(**EG**) which are consistent with these predictions.
- EG: {4-vectors, weights}

parton shower (PS)

- old wisdom of QCD
Konishi Ukawa Veneziano (1979)
Odorico (1980)
- systematic summation of large log's
in physical gauge (e.g. axial gauge)
interference diagrams = subdominant
stochastic (classical) branching
- naturally connect large/small Q^2

Proposed Strategy in PS-NLL

To construct **EG**, we are to go **beyond** the exact prediction of pert.QCD.

- Keep the prediction of pert.QCD.
- Matching with NLO matrix element
- Positiveness of branching (if possible)
- $LL > NLL$ (if possible)

Example(1) PDF, NS

$$\frac{d}{dt} f(x, Q^2) = \frac{\alpha_s(t)}{2\pi} \int_x^1 \frac{dy}{y} P(y) f(x/y, Q^2)$$

$$P(x) = P^{(0)}(x) + \frac{\alpha_s(t)}{2\pi} P^{(1)}(x) + \dots \quad P^{(0)} = C_F \frac{1+x^2}{1-x}$$

Fit by
experimental data

$$f(x, Q_0^2)$$

given

3 levels of MC

- Simple MC to solve DGLAP-eq.
- MC as branching process
- realistic MC as EG for incoming parton

MC to solve DGLAP

$$\frac{d}{dt} f(x, Q^2) = \frac{\alpha_s(t)}{2\pi} \int_x^1 \frac{dy}{y} P(y) f(x/y, Q^2)$$

$$\longrightarrow \Pi(Q_2^2, Q_1^2) = \exp \left[- \int_{Q_1^2}^{Q_2^2} \frac{dK^2}{K^2} \frac{\alpha_s(t_K)}{2\pi} \int_0^{1-\varepsilon} P(x) dx \right]$$

Non-branching probability from Q_1^2 to Q_2^2

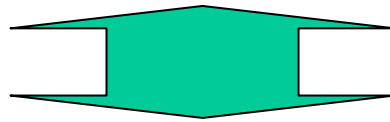
MC to determine $(-K^2, x)$ at each branching

MC to solve DGLAP

- **step.1** choose x_0 by initial distribution $f(x, Q_0^2)$
- **step.2** determine branch $-K^2$ by (Q^2, Q_0^2) , x_j by $P(x)$, repeat until $-K^2 > Q_{max}^2$
- **step.3** register $x = x_0 \times x_1 \times x_2 \times \dots$ as the x at Q^2
- This **should** agree with exact PDF Q^2 -dep.

MC to solve DGLAP

$$\Pi(Q_2^2, Q_1^2) = \exp \left[- \int_{Q_1^2}^{Q_2^2} \frac{dK^2}{K^2} \frac{\alpha_s(t_K)}{2\pi} \int_0^{1-\varepsilon} P(x) dx \right]$$



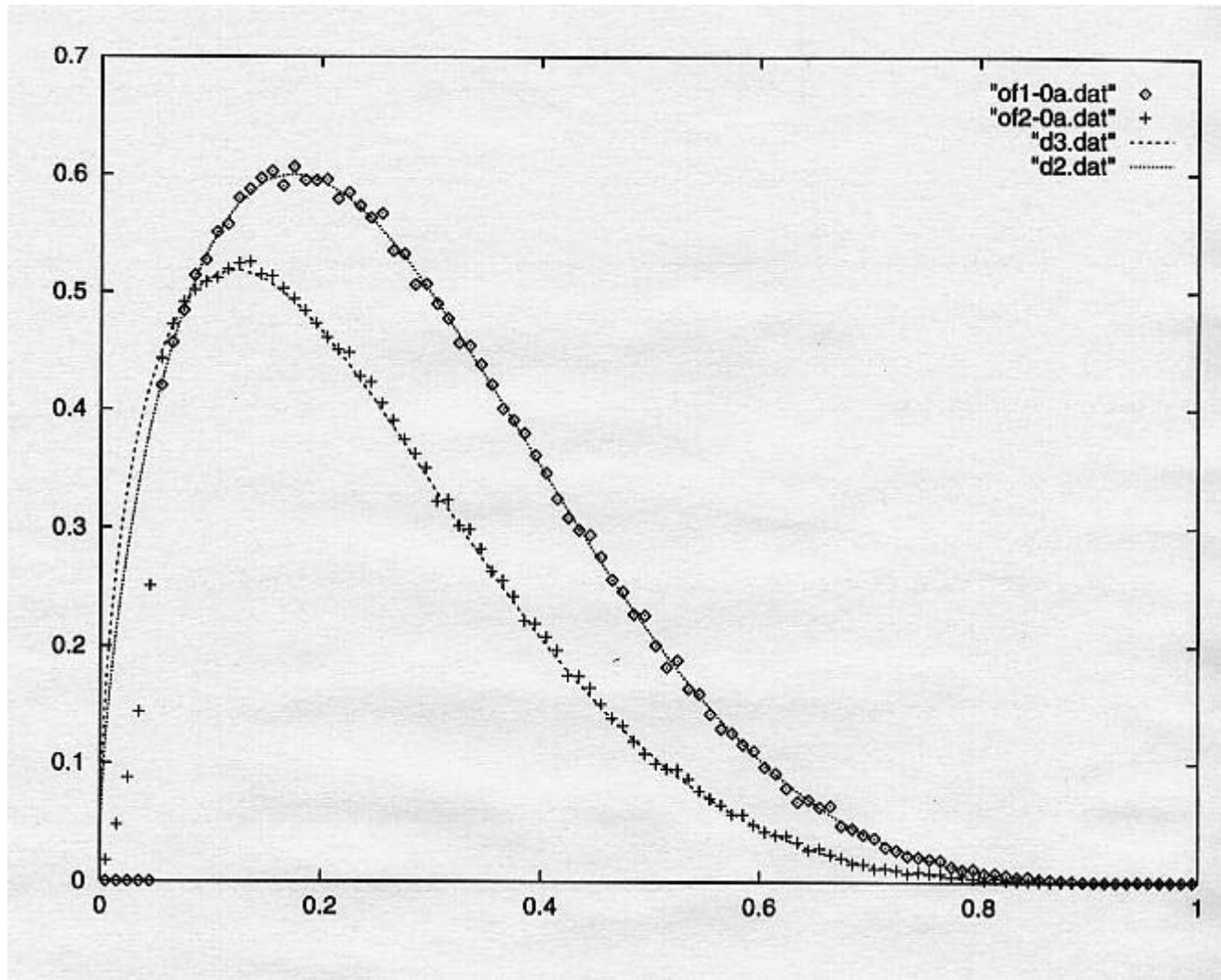
equivalent

QCD
prediction

$$\exp \left[- \int_{\alpha(\mu)}^{\alpha(Q)} \frac{d\alpha}{2\alpha} \frac{\gamma_n(\alpha)}{\beta(\alpha)/g} \right]$$

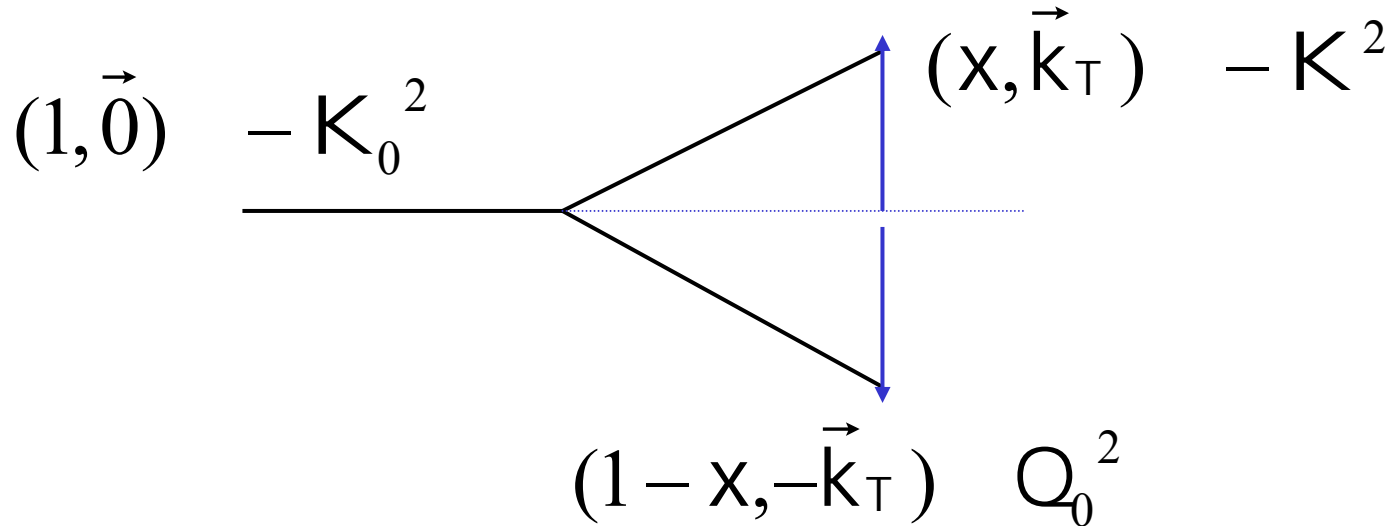
MRS99(mode-1) u-valence

$$Q^2 = 25\text{GeV}^2 \rightarrow 10^4\text{GeV}^2$$



(simple)
NLL-
PS

MC with branching



$$k_T^2 = -x(1-x)K_0^2 + (1-x)K^2 - xQ_0^2 > 0$$

MC with branching

$$-K_0^2 \ll -K^2 \Rightarrow x < 1 - \frac{Q_0^2}{-K^2}$$

$$\Pi(Q_2^2, Q_1^2) = \exp \left[- \int_{Q_1^2}^{Q_2^2} \frac{dK^2}{K^2} \frac{\alpha_s(t_K)}{2\pi} \int_0^{1-\varepsilon} P(x) dx \right]$$

$$\varepsilon = \frac{Q_0^2}{-K^2}$$

By this, $f(x, Q^2)$ receives some modification.

MC with branching

$$\mathcal{E} = \frac{Q_0^2}{-K^2}$$

New correction term appears to keep the pert.QCD prediction.

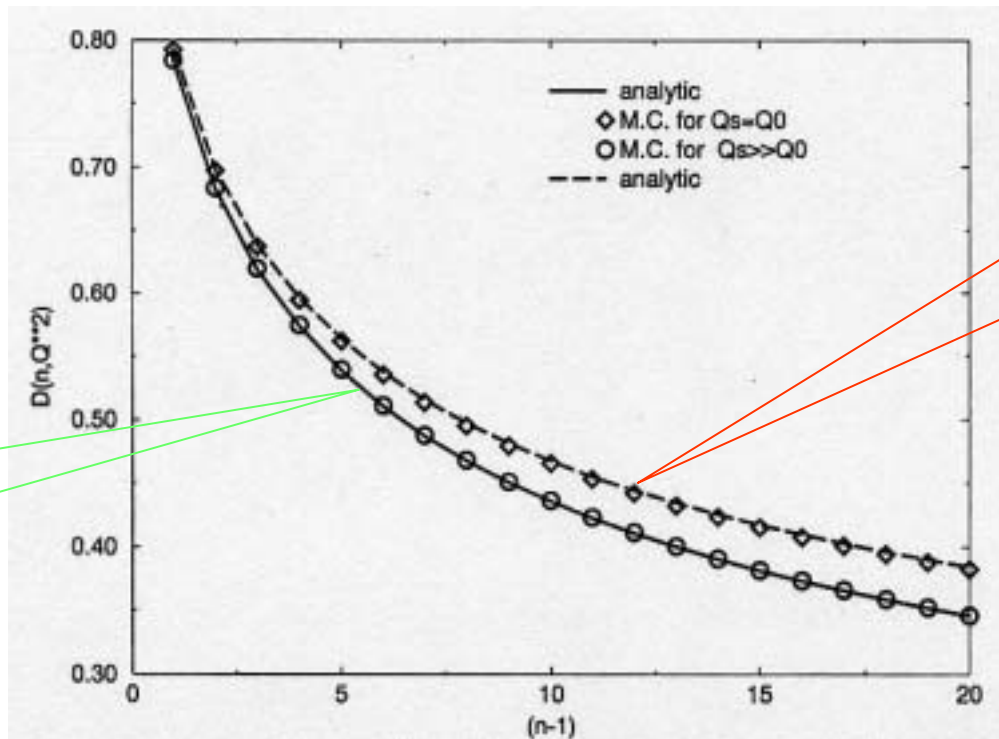


$$P(x)$$



$$P(x) - (\beta_0 / 2) \alpha_s(Q_0^2) \log(1-x) P(x)$$

moments of the SF



PS with
small cut

PS with K^2
dependent
cut

T.Munehisa, LL ($\alpha = 0.05$)

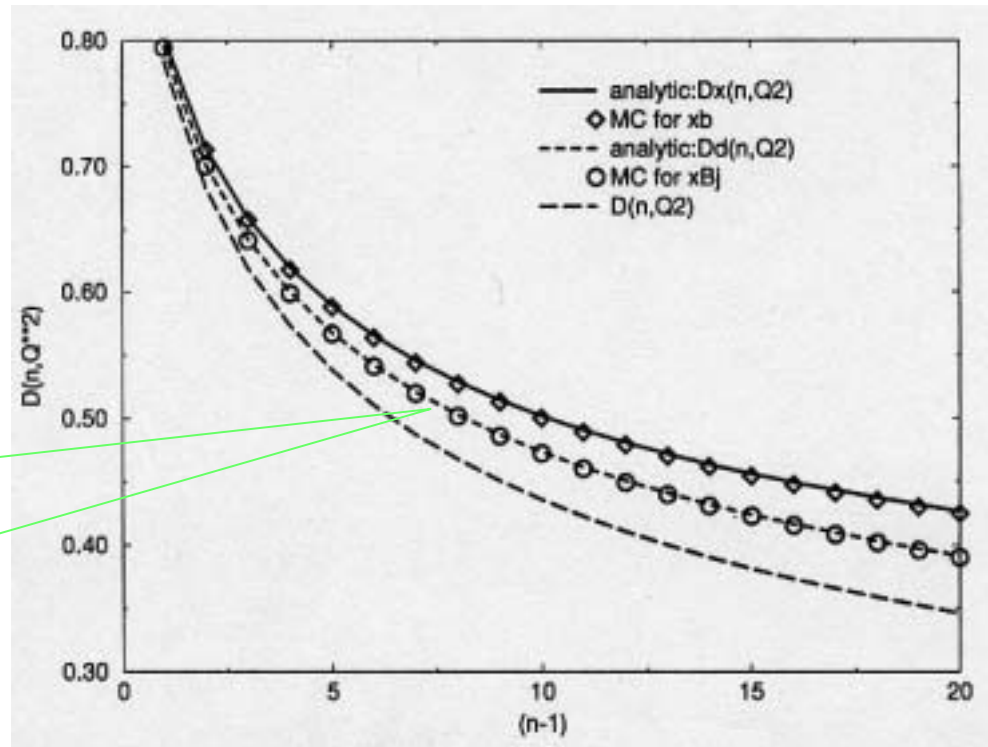
MC as EG

required items

- determine 4-vectors from $(-K^2, \mathbf{x})$
chosen at random
change ‘direction of parton’ ?
- What is the observed x_{Bj} ?
(Off-shell partons enter the collision.)

more correction terms

moments of the SF



PS for x_{Bj}

$$x_{Bj} = x(1 - t)$$

T.Munehisa, LL ($=0.05$)

Example(2) PDF, siglet

$P(x)$ Singular at $x=0$

$$\exp\left[-\int \frac{dK^2}{K^2} \frac{\alpha_s(K^2)}{2\pi} \int_0^{1-\varepsilon} P(x) dx\right]$$

- 1) Introduce cutoff
- 2) evolution of $x f(x, Q^2) \dots$
Momentum Conservation

**Study by
H. Tanaka**

siglet, $xf(x)$ evolution

$$\frac{d}{dt} f_q(x, t) = \frac{\alpha_s(t)}{2\pi} \int_x^1 [P_{qq}(y) f_q(x/y, t) + P_{qg}(y) f_g(x/y, t)] \frac{dy}{y}$$

$$\frac{d}{dt} f_g(x, t) = \frac{\alpha_s(t)}{2\pi} \int_x^1 [P_{gq}(y) f_q(x/y, t) + P_{gg}(y) f_g(x/y, t)] \frac{dy}{y}$$

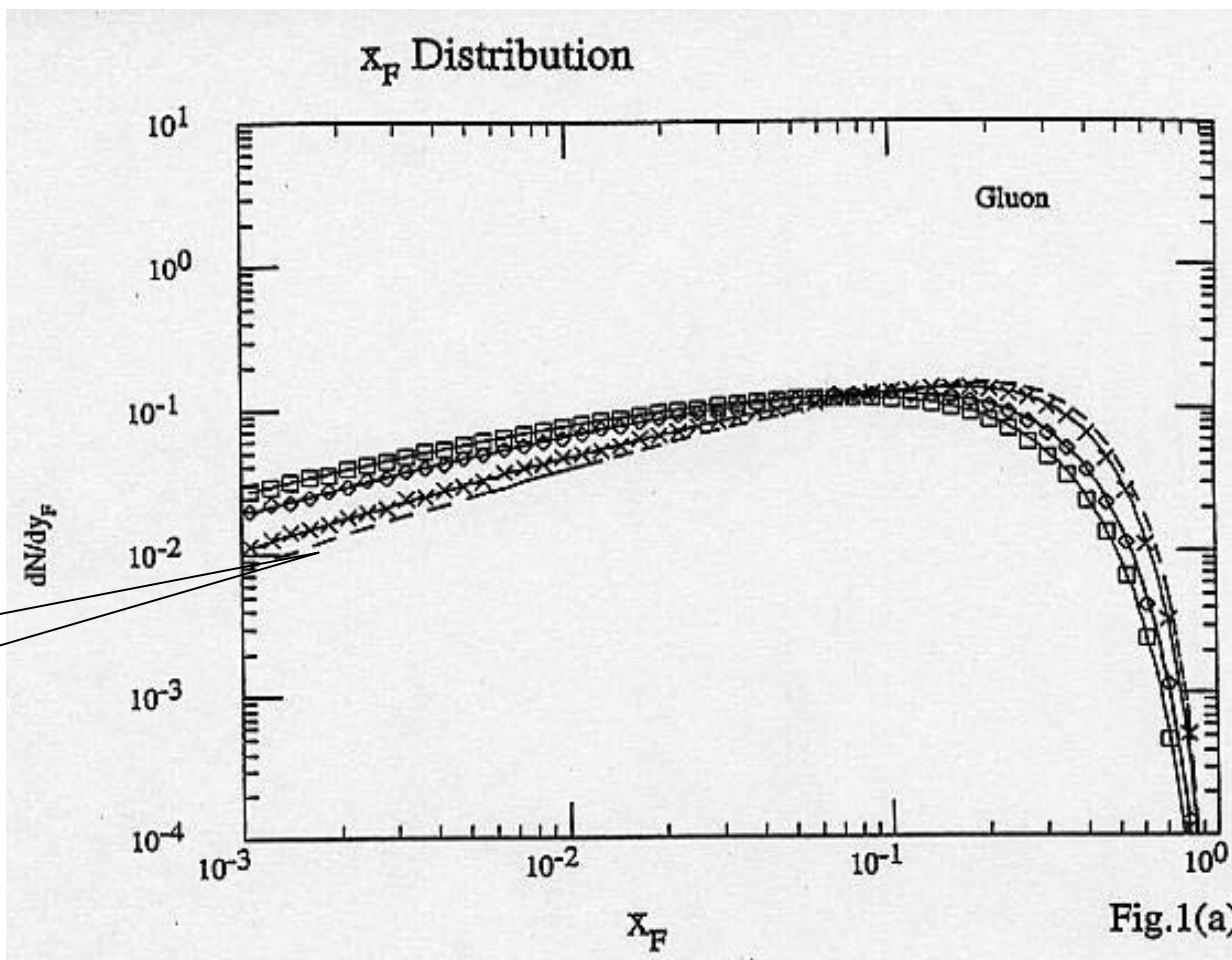
$$xf(x, t) \Rightarrow F(x, t)$$

$$\frac{d}{dt} F_q(x, t) = \frac{\alpha_s(t)}{2\pi} \int_x^1 [y P_{qq}(y) F_q(x/y, t) + y P_{qg}(y) F_g(x/y, t)] \frac{dy}{y}$$

$$\frac{d}{dt} F_g(x, t) = \frac{\alpha_s(t)}{2\pi} \int_x^1 [y P_{gq}(y) F_q(x/y, t) + y P_{gg}(y) F_g(x/y, t)] \frac{dy}{y}$$

gluon
(GRV98)

$$Q^2 = 10^1, 10^2, 10^3 \text{ GeV}^2$$



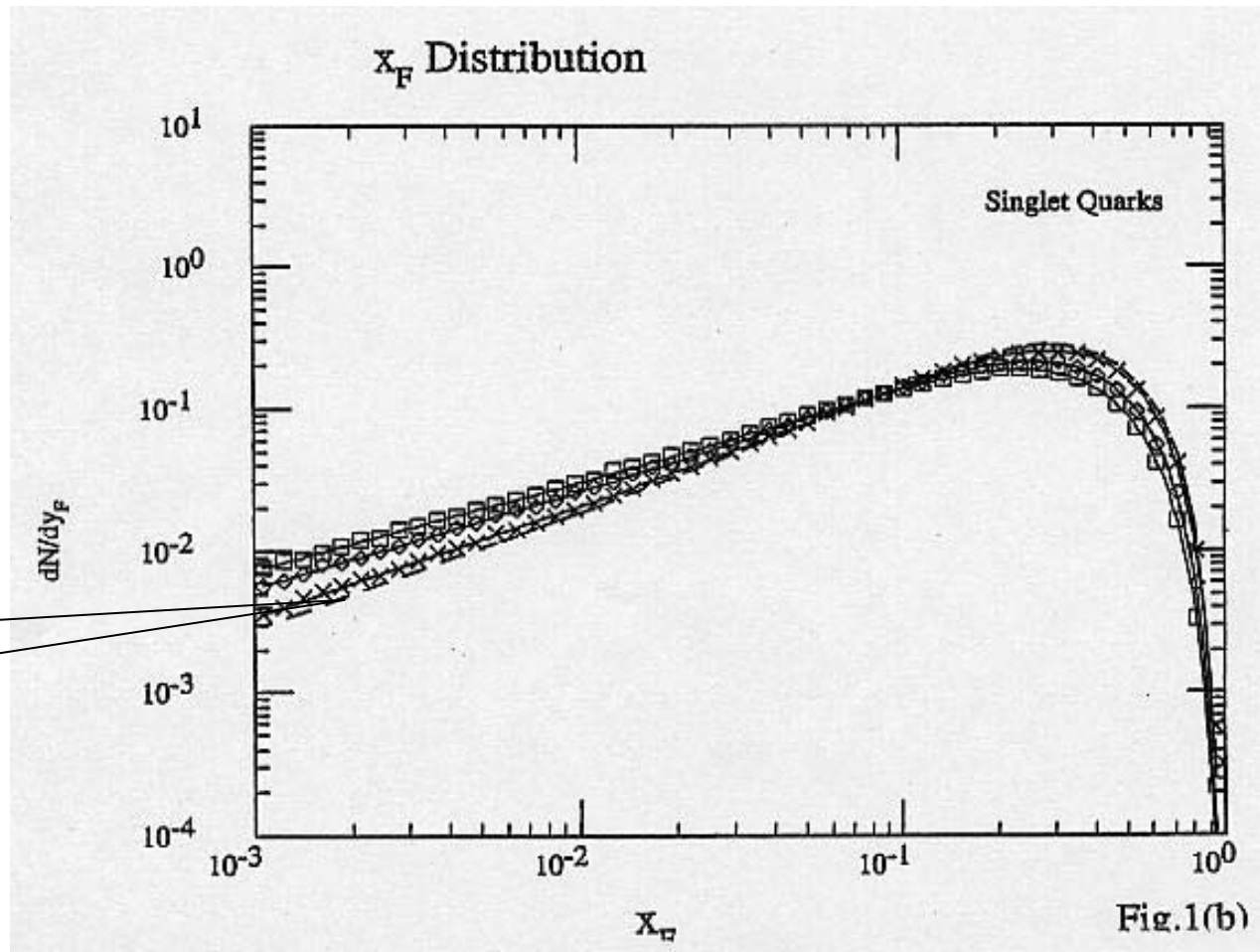
Input
 5 GeV^2

(simple)
**NLL-
PS**

H.Tanaka

singlet quark
(GRV98)

$$Q^2 = 10^1, 10^2, 10^3 \text{ GeV}^2$$

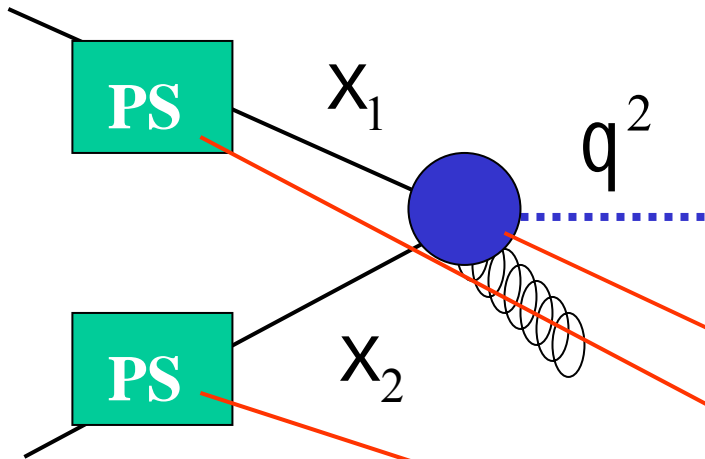


Input
 5 GeV^2

(simple)
**NLL-
PS**

H.Tanaka

Example(3) DY process



$$z = \frac{q^2}{S} = \frac{\tau}{x_1 x_2} \quad \tau = \frac{q^2}{S}$$

$$\tau \frac{d\sigma}{d\tau} = \sigma_0(S) \int dx_1 dx_2 \frac{1}{x_1 x_2} D(x_1, q^2) D(x_2, q^2) C(z, q^2)$$

$$\int_0^1 d\tau \frac{d\sigma}{d\tau} \tau^n = \sigma_0(S) D_n D_n C_n = F_n(q^2)$$

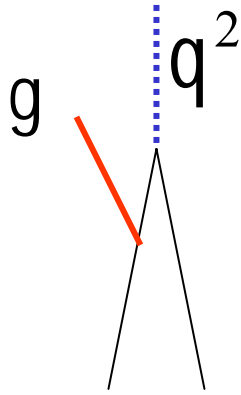
$$D_n = A_n \exp \left[- \int_{\alpha(\mu)}^{\alpha(Q)} \frac{d\alpha}{2\alpha} \frac{\gamma_n(\alpha)}{\beta(\alpha)/g} \right] \quad C_n = 1 + \frac{\alpha}{4\pi} B_n$$

$$\frac{F_n(q^2)}{F_n(q_0^2)} = \left(\frac{\alpha(q)}{\alpha(q_0)} \right)^{\gamma_n^{(0)}/2\beta_0} \left(1 + \frac{\alpha(q) - \alpha(q_0)}{4\pi} \left\{ B_n + 2 \frac{\gamma_n^{(1)}}{2\beta_0} - 2 \frac{\beta_1 \gamma_n^{(1)}}{2\beta_0^2} \right\} \right)$$

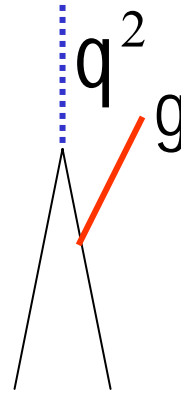
“scheme”
dependence

$$B \rightarrow B' \Rightarrow \gamma^{(1)} \rightarrow \gamma^{(1)'} = \gamma^{(1)} + \frac{B - B'}{\beta_0}$$

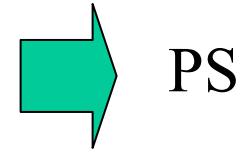
Hard ME
$$d\hat{\sigma} = Q_q^2 e^2 C_F g^2 \frac{2}{3} \left(\frac{t}{u} + \frac{u}{t} + 2 \frac{q^2 s}{tu} \right)$$



small $(-t)$



small $(-u)$



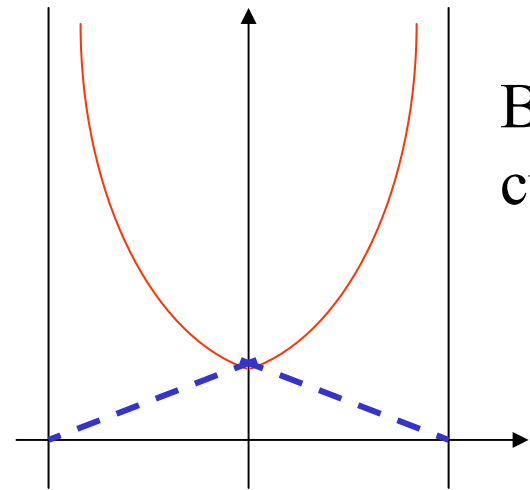
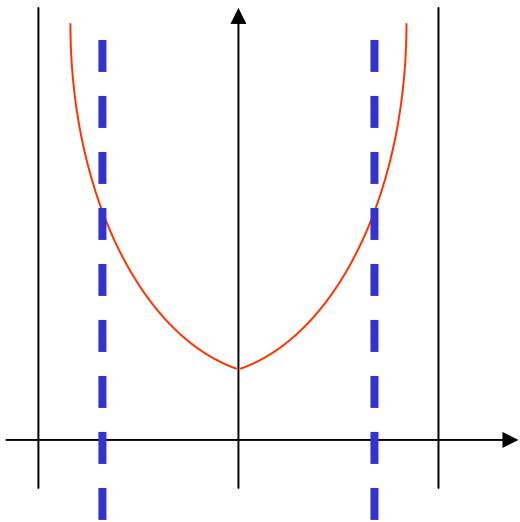
$$\delta = (-t, -u)_{\min} / s$$

$$\int d\hat{\sigma} = \frac{Q_q^2}{3} \sigma_{\mu\mu} \frac{dq^2}{q^2} \frac{\alpha}{4\pi} B'(z)$$

$$B'(z) = 4C_F \left[\frac{1+z^2}{1-z} (-\log(\delta / (1-z))) - (1-z) \right]$$

Modify (to avoid double counting)

$$\begin{cases} B(z) & \Rightarrow & B'(z) & \text{also modify P} \\ (-K^2)_{\max} = q^2 & \Rightarrow & (-K^2)_{\max} = \delta q^2 & \text{shower} \end{cases}$$



Better
cut ?

EG:mixture of * and *g

(intermediate) conclusion

- NLO generator with NLL-PS
- Connection to NLO-ME
- Technical study and test

continue to the next talk....